

27th Sept 2017

50 minutes

5 Pages

Open book, Open notes, Calculator, Ruler

100 total points

Read, think, plan, and then write.

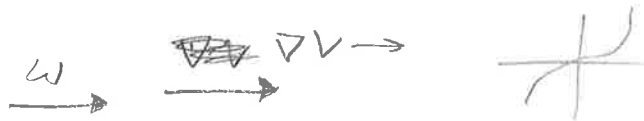
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Signature: _____

Date: _____

Multiple Choice Problems: [5 pts each]



1. A blob of fluid with vorticity $\omega = 1$ in the x-direction (i.e. $\omega = 1\hat{x} + 0\hat{y} + 0\hat{z}$) encounters accelerating flow in the x-direction (i.e. $V = x^3\hat{x}$). What happens to the vorticity magnitude?

<u>Increases</u>	Nothing	Decreases	Changes direction	Exponentially decays to zero
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2. Given the following airfoil, estimate the zero lift AOA in degrees.



$$\alpha = -\frac{2 \cdot 5}{130} \cdot \frac{180^\circ}{\pi} = -4.4$$

3. What is the divergence of a 2D flow with $V = x\hat{i} + xy\hat{j} + z^2\hat{k}$ at $z = 0$ and $x = -1$?

<u>0</u>	1/2	1	y	None of the above
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$$\nabla \cdot V = \frac{d}{dx}(x) + \frac{d}{dy}(xy) + \frac{d}{dz}(z^2)$$

$$1 + x^{-1} + 2z^0$$



4. For an NACA 64₃-418 airfoil at Re=6 million, what is the drag coefficient at +6 degrees AOA? The experimental data is plotted below (source: Theory of Wing Sections) 0.0075

60 counts	140 counts	80 counts	95 counts	None of the above
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5. What is the wingspan of a wing with: 250 square foot area, AR=10, and zero taper ratio?

$$AR = \frac{b^2}{S}$$

2500	50	35	25	0
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$$b = \sqrt{SAR}$$

6. For a 2D thin airfoil, what is the slope of the lift coefficient curve $dC_l / d\alpha$ [1/rad]?

0 deg	$1/\pi$	$4\sin^2(\alpha)\cos(\alpha)$	2π	None of the above
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7. Estimate the SSL stall speed of a Fokker Triplane (S=201 ft², W=1300 lbf) given the maximum lift coefficient is 2.2.

35 ft/s	45 mph	50 ft/s	55 ft/s	2480 ft/s
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$$L = W = \frac{1}{2} \rho V^2 S C_{L_{max}} \Rightarrow V = \sqrt{\frac{W \cdot 2}{\rho S C_{L_{max}}}}$$

8. An NACA 4321 has a

Thickness of 4%	Max Camber of 3% c	Max camber at 21% c	Max Thickness at 30% c	Max camber at 40%
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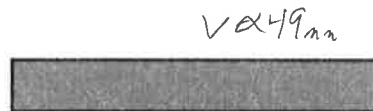
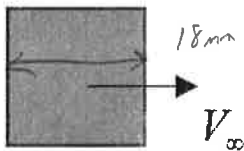
9. What is the air density in slug/ft³ at 80° F and 14.7 psi?

$$\frac{459.67 + 80}{14.7}$$

$$0.00228$$

$$\rho = \frac{P}{RT} = \frac{14.7 \text{ psi}}{1717 \text{ ft}^2/\text{s}^2 \cdot 539.67 \text{ R}} = \frac{14.7 \text{ lbf/ft}^2}{1717 \text{ ft}^2/\text{s}^2 \cdot 539.67 \text{ R}} = \frac{14.7 \text{ lbf/ft}^2}{925000 \text{ ft}^2/\text{s}^2 \cdot \text{R}} = \frac{14.7 \text{ lbf/ft}^2}{925000 \text{ ft}^2/\text{s}^2 \cdot \frac{1.355 \text{ slug} \cdot \text{ft}}{\text{lbf} \cdot \text{s}^2}} = \frac{14.7 \text{ lbf/ft}^2}{1250000 \text{ slug/ft}^3} = 0.01176 \text{ slug/ft}^3$$

10. In an incompressible flow at time t=0, you create a timeline-streakline box A at the freestream velocity. At a future time t=1, the box has distorted to box B. Compute the average pressure coefficient at B.

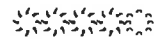


A

B

0	0.96	-7.3	-2π	None of the above
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$$C_p = 1 - \frac{V^2}{V_\infty^2} = 1 - \frac{49^2}{18^2} = -6.14$$



$\epsilon = 0.77\% \cdot 0.26 = 0.2$

$C_{L2} = 2\pi \frac{1+\epsilon}{1+\epsilon^2}$

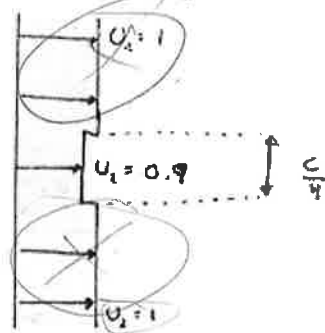
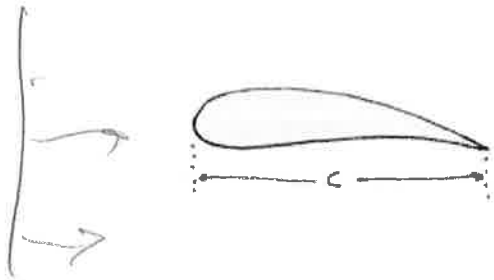
11. Given a 26% thick symmetrical Joukowski airfoil at 10 degrees AOA, estimate C_L ?

1.26	2π	$2\pi \cdot 1.15$	$2\pi \cdot 1.18$	72.5
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$C_L = C_{L\alpha} \alpha$

$2\pi \frac{1.2}{1.04} =$

12. An airfoil with a chord of "c" creates a uniform velocity of 0.9 with a thickness of c/4. The upstream velocity is $U_1=1$. Determine the sectional drag coefficient C_d .



$D = \int \rho U_2 (U_1 - U_2) dl$
 $= \rho \int 0.9 (1.0 - 0.9) dl$
 $D = \rho \int_{c/4} 0.09$

0.045

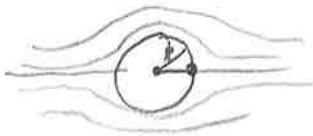
$= \rho \cdot 0.09 \cdot \frac{c}{4}$
 $C_D = \frac{D}{\frac{1}{2} \rho V^2 c} = \frac{2 \rho \cdot 0.09 \cdot \frac{c}{4}}{\rho c}$

13. What is the temperature at 10000 ft on a standard day?

10 F	23 F	59 F	223 F	483 F
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$59 - 0.0035$

14. Compute the velocity vector at $x=1$ and $y=0$ for the streamfunction



$\psi(r, \theta) = V_\infty r \sin(\theta) \left(1 - \frac{R^2}{r^2}\right)$ = F.S + D

0

15. What is the Reynolds number of a 10 inch airfoil operating at SSL and 100 ft/s?

$\frac{\rho V L}{\mu}$

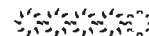
530 000

$Re = 6350 \frac{V^{ft/s}}{100} \cdot L^{ft}$

16. An aircraft is rotated to the following Euler angles: $\psi = 0$, $\theta = 90^\circ$, $\phi = 90^\circ$. Compute the angle of attack.

0 deg	45 deg	90 deg	180 deg	None of the above
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$\alpha = \tan^{-1} \frac{0}{0}$

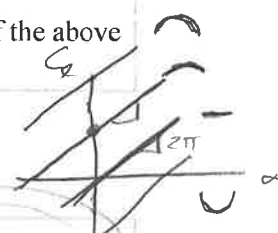


17. How does increasing camber affect the lift generation at a constant AOA (e.g. 0 degrees)?

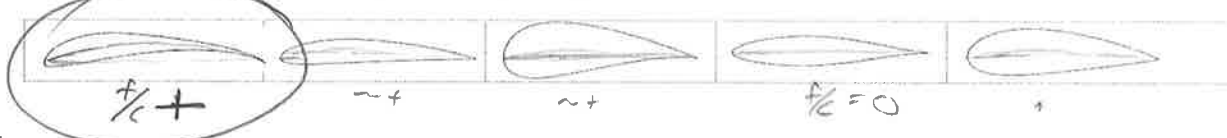
No effect	Increases C_l	Decreases C_l	Increases the Lift Slope C_{l_α}	None of the above
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18. Fundamentally, why do airfoils generate lift with a lift curve slope of 2π ?

2π is arbitrary	Thickness	Sharp TE	Kutta Joukowski $\rho V \Gamma$	I don't know
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19. Determine which airfoil has the most negative C_m



$C_m = -\frac{f}{c} \frac{1}{5}$

20. Identify the following aircraft part **exactly** by name. This is the part with the letters AH applied.

Vertical Stab



