

Happy Halloween (today)
and
All-Hallows Day (tomorrow)

100 total points

Read, think, plan, and then write.

University of Alabama Academic Honor Pledge:

I promise or affirm that I will not at any time be involved with cheating, plagiarism, fabrication, or misrepresentation while enrolled as a student at The University of Alabama. I have read the Academic Honor Code, which explains disciplinary procedures that will result from the aforementioned. I understand that violation of this code will result in penalties as severe as indefinite suspension from the University.

Signature: _____

Date: _____

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| # | # | # | # |
|---|---|---|---|

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Ⓟ

Multiple Choice Problems: Circle **EVERY** correct answer [4 pts each]

$AR = 1 \leq 4 - 5$

1. Estimate $C_{l,u}$ at $C_l = 2.0$ for a flat elliptical wing with an aspect ratio of 1 using Prandtl Lifting Line

| | | | | |
|-----------|-------------|------------|---------|--------------|
| A. 2π | B. $2\pi/3$ | C. $1/\pi$ | D. 0.01 | E. Not Valid |
|-----------|-------------|------------|---------|--------------|

2. A flat elliptical wing has an aspect ratio of 6. What is C_{D_i} at $C_l = -2.0$? Note the negative lift!

| | | | | |
|--------------|----------------|------|----------|----------------------|
| A. $-2/3\pi$ | B. 2122 counts | C. 0 | D. 0.106 | E. None of the above |
|--------------|----------------|------|----------|----------------------|

$C_{D_i} = \frac{C_l^2}{\pi AR}$

3. A flat tapered wing has an aspect ratio of 8 and taper ratio of 0.8. What is C_{D_i} at $C_l = 0.5$?

| | | | | |
|--|---|---------------------|---|----------------------|
| A. $1/32\pi$ <i>elliptical only</i> | B. 96 counts <i>elliptical / (8+1)</i> | C. 0 <i>zero</i> | D. 0.103 <i>elliptical / (8+1) shifted by 10</i> | E. None of the above |
|--|---|---------------------|---|----------------------|

Lesson 17
 $\delta \approx 0.038$
Fig on p. 5

4. For a subsonic flat linearly tapered wing, which taper ratio gives the lowest induced drag?

| | | | | |
|--------|---------|--------|--------|--------|
| 1. 0.0 | 2. 0.35 | 3. 0.5 | 4. 1.0 | 5. 1.5 |
|--------|---------|--------|--------|--------|

Lesson 17
Fig on p. 5

5. Compute the induced drag described by an upstream velocity of $u=10$ ft/s at SSL and a downstream velocity defined by:

$$v^2 + w^2 = \begin{cases} x & 0 < x < 1 \quad 0 < y < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$D = \frac{1}{2} \rho \iint (v^2 + w^2) dA = \frac{1}{2} \rho \int_0^1 \int_0^1 x dx dy = \frac{1}{4} \rho$$

| | | | | |
|--------------|-------------|-------------|-----------------------|----------------------|
| A. $\pi\rho$ | B. 5 counts | C. $\rho/4$ | D. $\frac{2\pi}{100}$ | E. None of the above |
|--------------|-------------|-------------|-----------------------|----------------------|

6. Which XFOIL command sequence would simulate a NACA 0012 at $Re=60000$ at $AOA=5^\circ$?

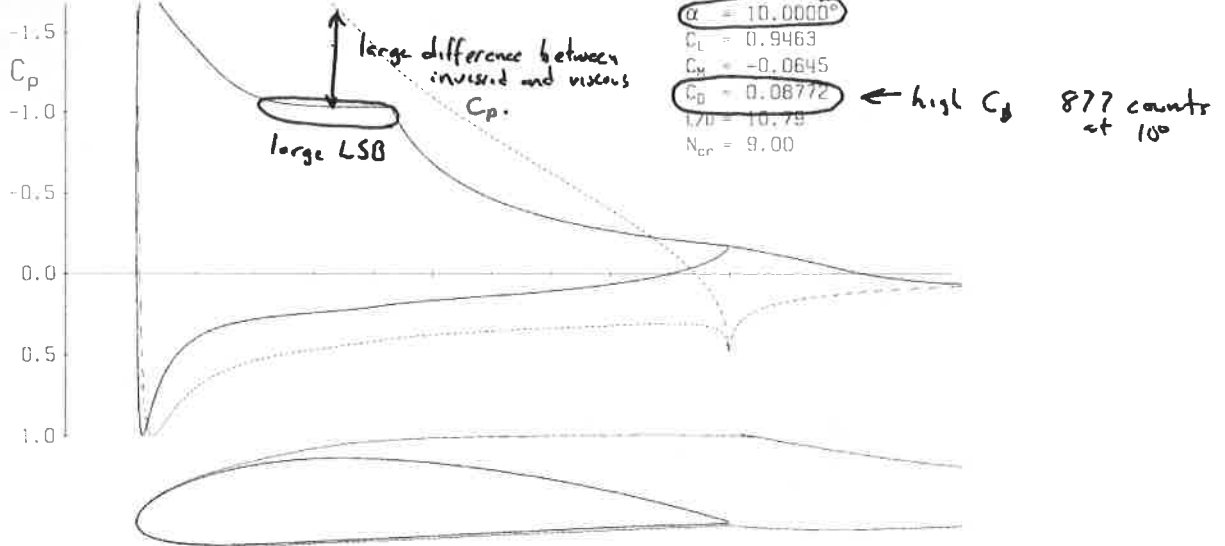
| | | | | |
|--|---|---|---|----------------------|
| A. naca 0012 oper visc 60000 alfa 5 hard | B. naca 0012 oper visc 60000 alpha 5 | C. load naca0012 ppar 280 oper visc 60000 alpha 5 | D. naca 0012 ppar N 280 oper visc 60000 aseq 5 | E. None of the above |
|--|---|---|---|----------------------|

hard copy

spelling

sequence

7. For an NACA 4414 airfoil simulated with XFOIL, determine the most likely Reynolds number?



- | | | | | |
|---------------------------|----------|-----------|---------------------|---------------------|
| A. Inviscid <i>BL.</i> | B. 60000 | C. 600000 | D. $6.0 \cdot 10^6$ | E. $6.0 \cdot 10^7$ |
|---------------------------|----------|-----------|---------------------|---------------------|

HW was at 200k

8. Where is the shed vorticity in the wake highest?

- | | | | | |
|------------------------------|------------------------------|-------------------|------------------------------------|----------------------|
| A. Where Γ is highest | B. At a wing geometry change | C. At the wingtip | D. Where $ d\Gamma/dy $ is largest | E. None of the above |
|------------------------------|------------------------------|-------------------|------------------------------------|----------------------|

9. For a delta wing, increasing the leading edge sweep angle from 50 to 70 degrees tends to

- | | | | | |
|-------------------------|----------------------------|--------------------------|--------------------------|----------------------------------|
| A. Increase $C_{L,max}$ | B. Increase $C_{L,\alpha}$ | C. Increase induced drag | D. Increase Aspect Ratio | E. Increase the vortex burst AOA |
|-------------------------|----------------------------|--------------------------|--------------------------|----------------------------------|

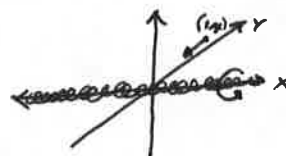
10. For a transport aircraft with flaps up at low altitudes, where are contrails likely to 1st occur?

- | | | | | |
|--------------|-----------------|------------|--------------|--------------|
| A. Wing tips | B. Jet exhausts | C. Strakes | D. Wing root | E. Flap tips |
|--------------|-----------------|------------|--------------|--------------|

11. What is the velocity vector at $(x,y,z)=(1,0,1)$ consistent with an infinite vortex of strength 2π along the x axis (i.e. positive vortex about positive x direction)?

- | | | | | |
|------------|-------------|------------|---------------|-----------------|
| A. (0,0,0) | B. (0,-1,0) | C. (0,1,0) | D. (0,-1/2,0) | E. (0,-0.707,0) |
|------------|-------------|------------|---------------|-----------------|

$$V = \frac{\Gamma}{2\pi h}$$



12. Which wing geometries tend to have higher C_l loading near the wing root?

- | | | | | |
|--------------|------------------|------------|-----------|---------------------|
| A. Aft swept | B. Forward swept | C. Washout | D. Washin | E. Elliptical wings |
|--------------|------------------|------------|-----------|---------------------|

13. Circle the phenomena described: Drag due to lift

- | | | | | |
|-----------------|----------------|-----------------|---------------------|-----------------|
| A. Induced Drag | B. Adverse Yaw | C. Proverse Yaw | D. Aileron Reversal | E. Not possible |
|-----------------|----------------|-----------------|---------------------|-----------------|

14. If a flat non-elliptical $\lambda = 1$ wing is designed to give an Oswald efficiency factor for 1 (i.e. mimicking an elliptical wing), what is true?

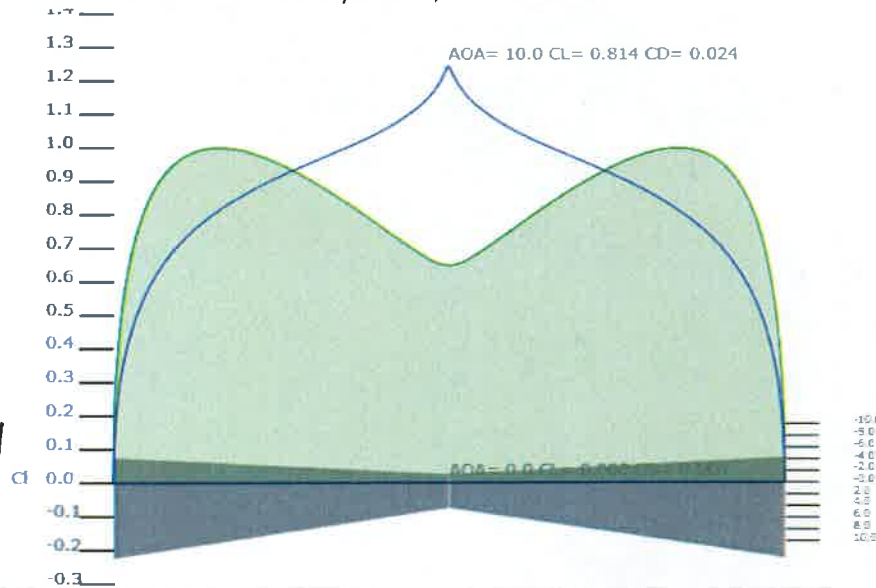
- | | | | | |
|-----------------|---|-------------------------------------|---|--|
| A. Not possible | B. airfoil sections must be thicker at the root | C. The wing twist varies with span. | D. The quarterchord downwash is constant. | E. The zero lift line varies with span |
|-----------------|---|-------------------------------------|---|--|

15. Given the following lift distribution at AOA=10 for the following AR=10 wing with $C_L=0.814$, $C_D=0.024$ and $\lambda = 3$, estimate the Oswald Efficiency Factor, e.

$$C_D = \frac{C_L^2}{\pi AR e}$$

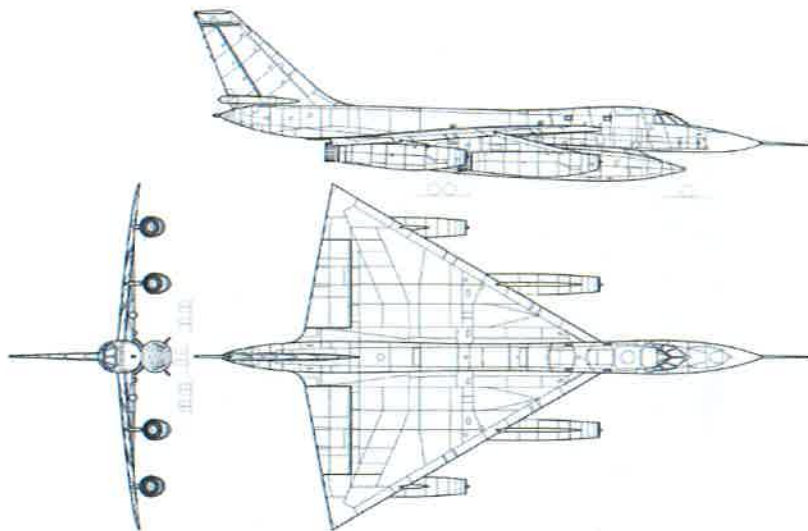
$$e = \frac{C_L^2}{\pi AR C_D}$$

$$= \frac{(0.814)^2}{\pi \cdot 10 \cdot 0.024}$$



- | | | | | |
|---------|---------|---------|---------|----------------------|
| A. 0.88 | B. 0.93 | C. 1.08 | D. 1.14 | E. None of the above |
|---------|---------|---------|---------|----------------------|

16. [20 pts] Estimate the takeoff speed in ft/s of a B-58 at 150000 lbf at AOA=14 degrees at SSL. The leading edge sweep is 60°. The aspect ratio is 2.09. The wing area is 1542 sq-ft. Hint: $V > 200$ mph



(5) $K_p \approx 2.25$
 $K_v \approx 2.9$

(5)
$$C_L = K_p \sin \alpha \cos^2 \alpha + K_v \cos \alpha \sin^2 \alpha$$

$$= 2.25 \sin 14^\circ \cos^2 14^\circ + 2.9 \cos 14^\circ \sin^2 14^\circ$$

$$= 0.677$$

(5)
$$L = W = \rho S C_L = \frac{1}{2} \rho V^2 S C_L$$

$$V^2 = \frac{2W}{\rho S C_L} \Rightarrow V = \sqrt{\frac{2W}{\rho S C_L}}$$

$$V = \sqrt{\frac{2 \cdot 150000 \text{ lbf}}{0.00237 \text{ slug/ft}^3} \cdot \frac{\text{ft}^2}{1542} \cdot 0.677} \cdot \frac{\text{slug ft}}{16 \text{ s}^2}$$

(5)
$$V = 348 \text{ ft/s}$$

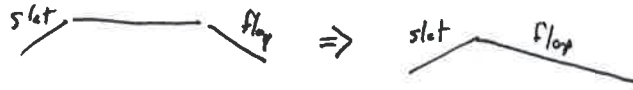
≈ 240 mph

17. [20 pts] Estimate the lift coefficient of a thin cambered airfoil at AOA=0. The airfoil is composed of two linear parts. The maximum camber is 10% at the quarterchord.



Short method?

Lesson 13 slot-flop



$$\theta_{sf} = \alpha \cos\left(1 - 2\frac{x}{c}\right) = \alpha \cos\left(1 - 2 \cdot 0.25\right) = 1.047 \text{ rad}$$

$$\delta_s = \alpha \tan\left(\frac{10}{25}\right) = +0.38$$

$$\delta_f = \alpha \tan\left(-\frac{10}{75}\right) = +0.13255$$

$$C_L = 2\pi\alpha + 2\pi\delta_f\left(1 - \frac{\theta_f}{\pi} + \frac{\sin\theta_f}{\pi}\right) + 2\pi\delta_s\left(-\frac{\theta_s}{\pi} + \frac{\sin\theta_s}{\pi}\right)$$

$$= 2\pi \cdot 0 + 2\pi \cdot 0.13255 \left(1 - \frac{1.047}{\pi} + \frac{\sin 1.047}{\pi}\right) + 2\pi \cdot 0.38 \left(-\frac{1.047}{\pi} + \frac{\sin 1.047}{\pi}\right)$$

$$= 0.647$$

Traditional Method

$$A_0 = \alpha - \frac{1}{\pi} \int_0^{\theta_{sf}} \frac{dz}{dx} d\theta = \alpha - \frac{1}{\pi} \int_0^{1.047} 0.4 d\theta - \frac{1}{\pi} \int_{1.047}^{\pi} -0.13255 d\theta$$

$$= \alpha - \frac{1}{\pi} (0.4 \cdot 1.047) + \frac{1}{\pi} (0.13255 (\pi - 1.047))$$

$$= \alpha - 0.0444$$

$$A_1 = \frac{2}{\pi} \int_0^{1.047} 0.38 \cos\theta d\theta + \frac{2}{\pi} \int_{1.047}^{\pi} 0.13255 \cos\theta d\theta$$

$$= \frac{2}{\pi} (0.38 (\sin 1.047 - \sin 0)) + \frac{2}{\pi} (0.13255 (\sin \pi - \sin 1.047)) = 0.294$$

$$C_L = 2\pi(-0.0444) + \pi(0.294) = 0.645$$