

Lessons 12 - 18

Anderson book Chap 4-5

University of Alabama Academic Honor Pledge:

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Signature: _____

Date: _____

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Multiple Choice Problems: Circle **EVERY** correct answer [3 pts each]

$$1 + \frac{2}{AR} = 1 + \frac{2}{8} = \frac{2\pi}{1.25}$$

1. A flat elliptical wing has an aspect ratio of 8. What is C_{D_i} ? $\frac{dC_L}{dC_D}$

A.	B.	C.	D.	E. None of the above
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5.026 counts

2. A flat elliptical wing has an aspect ratio of 8. What is C_{D_i} at $C_L = 0.5$?

$$C_{D_i} = \frac{C_L^2}{\pi AR} = 99 \text{ counts}$$

A.	B.	C.	D.	E. None of the above
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3. A flat tapered wing has an aspect ratio of 8 and taper ratio of 0.5. What is C_{D_i} at $C_L = 0.5$?

$$C_{D_i} = \frac{C_L^2}{\pi A e} (1 + \delta) \approx 1.015$$

A.	B.	C.	D.	E. None of the above
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100 counts

4. For a subsonic flat linearly tapered wing, which taper ratio gives the lowest induced drag?

1. 0.0	2. 0.3	3. 0.5	4. 1.0	5. 1.5
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5. Compute the induced drag described by an upstream velocity of $u=1$ at SSL and a downstream velocity defined by:

$$v^2 + w^2 = \begin{cases} 0.1 & r^* < 1 \\ 0 & \text{otherwise} \end{cases}$$

0.000372

$$v^2 + w^2 = 0.1$$

$$v^2 + w^2 = 0$$

$$D = \frac{1}{2} \rho \iint v^2 + w^2 dA = \frac{1}{2} \rho \pi r^2 0.1$$

A.	B.	C.	D.	E. None of the above
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5. Why is the lift distribution $\Gamma(y) = y$ not physically possible for a finite wing of span $b=1$?

A. Negative Γ	B. Not elliptical	C. Asymmetric	D. Infinite velocities	E. None of the above
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6. Determine the lift coefficient of a wing of span $b=2$ given the following bound vortex distribution:

$$C_L = \frac{\int \Gamma dy}{\frac{1}{2} \rho V S} \quad \Gamma(y) = \cos\left(\pi \frac{y}{b}\right)$$



A. $\frac{8}{\pi V S}$	B.	C.	D.	E. None of the above
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$$\frac{2\Gamma}{VS} = \int_{-1}^1 \cos\left(\pi \frac{y}{b}\right) dy$$

$$\frac{4 \cdot 2}{\pi VS} = \frac{8}{\pi VS}$$

7. Why do increasing lengths of contrails indicate the increasing possibility of stormy weather?

- | | | | | |
|--|---|---|---------------------------------------|----------------------|
| A. Combustion provides ionic paths for lightning | B. Vortices create an unstable atmosphere | C. Contrails increase atmospheric heating | D. Atmospheric moisture is increasing | E. None of the above |
|--|---|---|---------------------------------------|----------------------|

8. In the following figure, where is the shed vorticity in the wake highest?

- | | | | | |
|--|---|---|---------------------------------------|----------------------|
| F. Combustion provides ionic paths for lightning | G. Vortices create an unstable atmosphere | H. Contrails increase atmospheric heating | I. Atmospheric moisture is increasing | J. None of the above |
|--|---|---|---------------------------------------|----------------------|



$$\gamma = -\frac{d\Gamma}{dy}$$

9. A finite wing with AR=10 has the following Fourier coefficients. What is the lift coefficient?

$$A_n = 0.1^n$$

$$\pi AR a_1 = \pi AR \cdot 0.1$$

$$\pi$$

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|----|----|----|----|----|
| A. | B. | C. | D. | E. |
|----|----|----|----|----|

10. In a panel method for an airfoil, where are numerical instabilities most likely to occur?

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|------------------|-----------------|---------------|----------------------|----------------------|
| A. Trailing Edge | B. Leading Edge | C. Freestream | D. Maximum thickness | E. None of the above |
|------------------|-----------------|---------------|----------------------|----------------------|

11. Where is the theoretical aerodynamic center of a flying wing?

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|------------------|---------------|------------------|-----------------|----------------------|
| A. Neutral point | B. Half chord | C. Quarter Chord | D. Leading edge | E. None of the above |
|------------------|---------------|------------------|-----------------|----------------------|

12. For a delta wing, increasing AOA tends to move the vortex burst point

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|------------|--------|-------------|-------------------|------------------|
| A. Forward | B. Aft | C. Outboard | D. Below the wing | E. Does not move |
|------------|--------|-------------|-------------------|------------------|

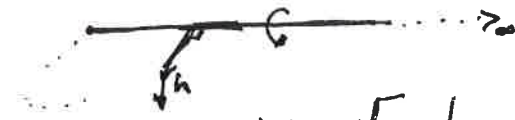
13. For attached flow over an NACA 0012 airfoil, where is the vorticity concentrated?

- | | | | | |
|---------------|------------------|---------|---------------------|----------------------------|
| A. Everywhere | B. Quarter Chord | C. Wake | D. Near the surface | E. Nowhere. Zero vorticity |
|---------------|------------------|---------|---------------------|----------------------------|



14. For a high speed aircraft at high altitudes, where are contrails likely to 1st occur?

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|--------------|-----------------|------------|--------------|--------------|
| A. Wing tips | B. Jet exhausts | C. Strakes | D. Wing root | E. Flap tips |
|--------------|-----------------|------------|--------------|--------------|



$$V = \frac{\Gamma}{4\pi h}$$

$$= \frac{1}{4\pi}$$

15. What is the velocity imposed by a semi-infinite vortex of strength 1 at a distance $h=1$?

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|----|----|---------------------|----|----|
| A. | B. | C. $\frac{1}{4\pi}$ | D. | E. |
|----|----|---------------------|----|----|

16. Which wing geometries tend to have higher C_l loading near the wingtips?

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|--------------|------------------|------------|-----------|---------------------|
| A. Aft swept | B. Forward swept | C. Washout | D. Washin | E. Elliptical wings |
|--------------|------------------|------------|-----------|---------------------|

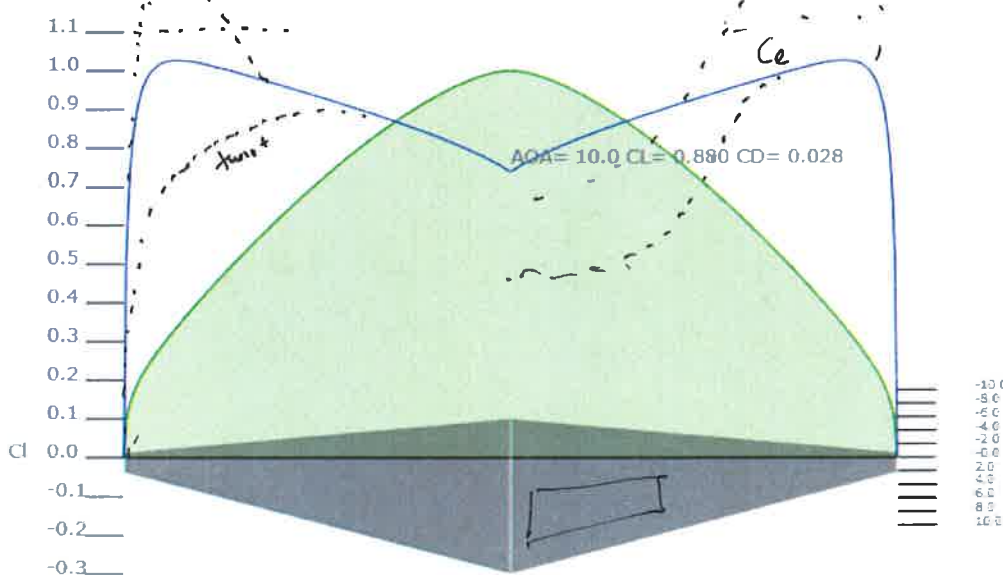
17. Circle the phenomena described: A positive roll moment creates an opposite yaw moment.

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|-----------------|----------------|-----------------|---------------------|-----------------|
| A. Induced Drag | B. Adverse Yaw | C. Proverse Yaw | D. Aileron Reversal | E. Not possible |
|-----------------|----------------|-----------------|---------------------|-----------------|

18. Circle the Helmholtz vortex filament theorems

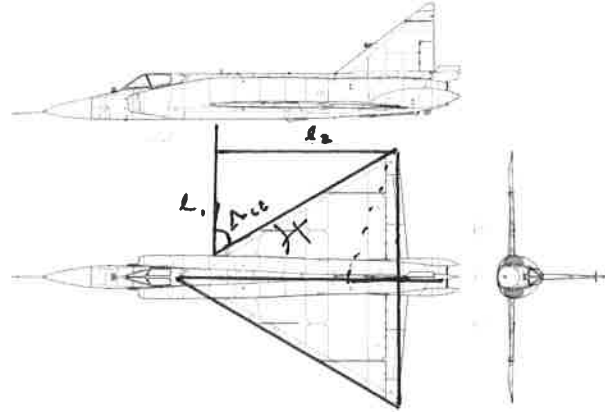
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|-------------------------------|---------------------------------------|---------------------------------|-------------------------------------|----------------------------------|
| A. Constant filament strength | B. Filaments never end within a fluid | C. Filaments convect downstream | D. Filaments shapes remain constant | E. Filaments decay exponentially |
|-------------------------------|---------------------------------------|---------------------------------|-------------------------------------|----------------------------------|

19. Given the following lift distribution at $AOA=10$ degrees, which wing modifications are likely to improve flight performance and pilot workload during high AOA maneuvers near stall? Assume that the airfoil section has a maximum lift coefficient of $C_{l,max} = 1.1$



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|-----------|------------|--------------|-----------------------------|--|
| A. Washin | B. Washout | C. Aft sweep | D. Decrease the taper ratio | E. Inboard spoilers deflected 10 degrees |
|-----------|------------|--------------|-----------------------------|--|

20. Estimate the lift to drag ratio (CL/CD) of an F-102 Delta Dagger at AOA=35 degrees?



$$\tan \Lambda = \frac{24}{14} = 60^\circ$$

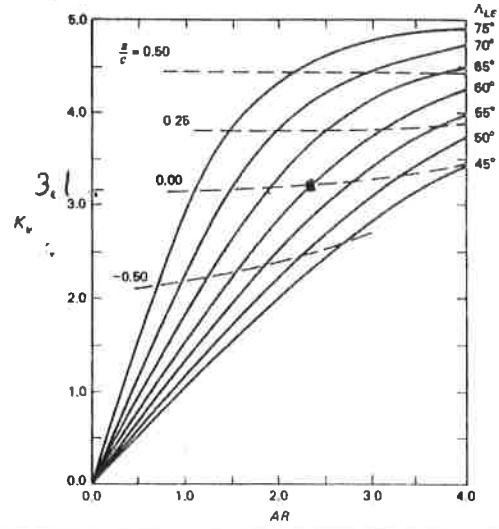
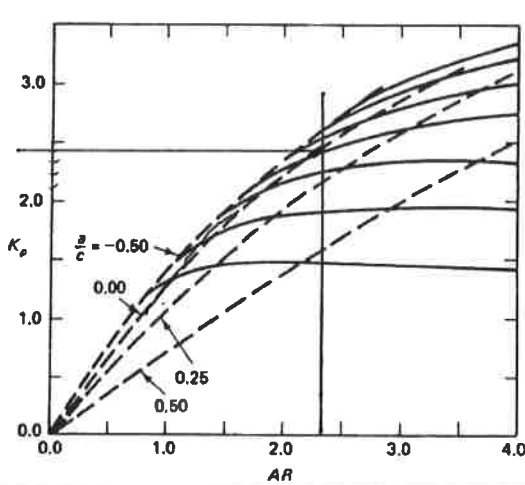
$$\bar{c} = \frac{30}{2} = 15$$

$$b = 34$$

$$S = 510$$

$$AR \approx 2.3$$

2.4



- | | | | | |
|----|----|----|----|----|
| A. | B. | C. | D. | E. |
|----|----|----|----|----|

$$K_p = 2.4 \quad K_v = 3.1$$

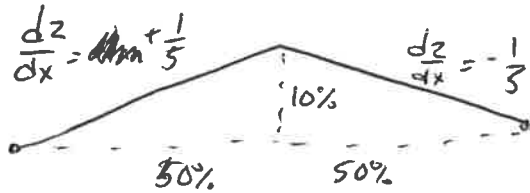
$$\sin 35^\circ = 0.5735$$

$$\cos 35^\circ = 0.8192$$

$$\frac{C_L = K_p \sin \alpha \cos^2 \alpha + K_v \cos \alpha \sin^2 \alpha}{C_D = K_p \sin^2 \alpha \cos \alpha + K_v \sin^3 \alpha} = \frac{1.759}{1.231}$$

$$= 1.43$$

21. [20 pts] Estimate the lift, drag, and moment of a thin cambered airfoil at $\text{AOA}=0$. The airfoil is composed of two linear parts. The maximum camber is 10% at the midchord.



$$A_0 = \alpha - \frac{1}{\pi} \int_0^{\pi/2} \frac{1}{5} d\theta - \frac{1}{\pi} \int_{\pi/2}^{\pi} -\frac{1}{5} d\theta$$

$$= \alpha - \frac{1}{\pi} \frac{1}{5} \frac{\pi}{2} + \frac{1}{\pi} \frac{1}{5} \left(\pi - \frac{\pi}{2} \right)$$

$$= \alpha - \frac{1}{10} + \frac{1}{10}$$

$$A_1 = \frac{2}{\pi} \int_0^{\pi/2} \frac{1}{5} \cos \theta d\theta + \frac{2}{\pi} \int_{\pi/2}^{\pi} -\frac{1}{5} \cos \theta d\theta = \frac{2}{\pi} \frac{1}{5} \cdot 2 = \frac{4}{5\pi}$$

$$A_2 = \frac{2}{\pi} \int_0^{\pi/2} \frac{1}{5} \cos 2\theta d\theta + \frac{2}{\pi} \int_{\pi/2}^{\pi} -\frac{1}{5} \cos 2\theta d\theta = 0$$

$$C_l = 2\pi A_0 + \pi A_1 = 2\pi \left(\alpha \right) + \frac{4}{5}$$

$$= \frac{4}{5} = \boxed{0.8}$$

$$\boxed{C_d = 0}$$

$$C_m = -\frac{\pi}{4} (A_1 - A_2) = -\frac{1}{5} = \boxed{-0.2}$$