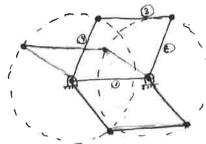
Lesson &

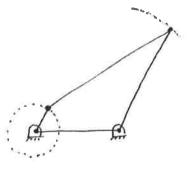
Longitudinal Control

Mechanisms

4 bar linkage

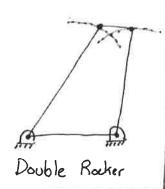


Drug Link

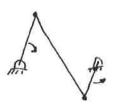


Crank Rocker

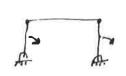
ON MANO



The rotation direction is not always the same for a drag like .



Anti- parallel



parallel

Gruebler's Equation (2D)

· Each link has 3 Degrees of Freedom (DOF)



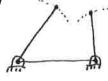
2 translate 1 rotale

· Each pivot subtract, 2 DOF



The total system DOF = 3(N-1)-2p

Example:



How many DOF?

3 links > N=3
2 pivols = p=2

Dof =
$$3(N-1)-2P$$

= $3(3-1)-2.2$
 $6-4=2$

Example



3 Links => 3(3-1) - 2.3 = 0 3 pivots triangles are abble

Example

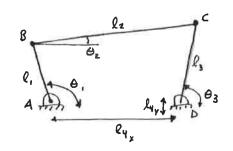


9# links = 3(9-1)-2.7 = 10

How many DOF?

Over constrained!

General 4 bor

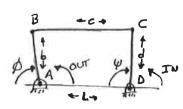


Assume system is connected

X direction: $l_1 \cos \theta_1 + l_2 \cos \theta_2 + l_3 \cos \theta_3 - l_{4x} = 0$ Y direction: $l_1 \sin \theta_1 + l_2 \sin \theta_2 + l_3 \sin \theta_3 - l_{4y} = 0$

These are constraints but they don't give us information on $\theta_1 = f(\theta_3)$

Freudenstein Equation (notice the angle convention!)



Consider the term AB =5 the vector from A to B

AB = CD = DC =

From continuity, AB+BC = AD+DC

Solve for BC = AD+DC-AB = - (DA+CD+AB)

Freudensteins insight was to take the dot product of BC with BC.

Find terms for location of B,C (axuning mechanism is aligned with x axis at A and U)

Simplify BC. BC = c2 !! Such that

$$C^2 = [1 + b\cos\phi - d\cos\psi, -b\sin\phi + d\sin\psi] \cdot [1.11]$$

After some simplification

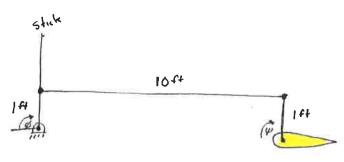
$$R_1 \cos \phi = R_2 \cos \phi + R_3 = \cos (\phi - \psi)$$

$$R_1 = \frac{1}{2}$$
 $R_2 = \frac{1}{2}$ $R_3 = \frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2$

43 unknowns

43 equations - You need to specify 34 postions.

Example



$$R_1 = \frac{1}{b} = 10$$

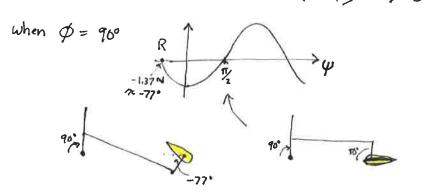
$$R_2 = \frac{1}{b} = 10$$

$$R_3 = \frac{100 + 1 - 100 + 1}{2} = 1$$

Freudenstein

$$10\cos\phi - 10\cos\psi + 1 = \cos(\phi - \psi)$$

Residual = $10\cos\varphi - 10\cos\psi + 1 - \cos(\varphi - \psi) \rightarrow 0$

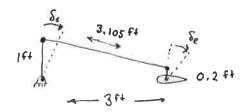


What about the gearing ratio? $\frac{d\psi}{d\phi}$ Take $\frac{d}{d\phi}$ of Freedonstein while rememberin, that $\psi = f(\phi)$ $\frac{d}{d\phi}(R_1\cos\phi - R_2\cos\psi + R_3 = \cos(\phi - \psi))$ $= -R_1\sin\phi \frac{d\phi}{d\phi} + R_2\sin\psi \frac{d\psi}{d\phi} + 0 + \sin(\phi - \psi) \frac{d\phi}{d\phi}(\phi - \psi)$ Solve for $\frac{d\psi}{d\phi}$

$$\frac{d\psi}{d\theta} = \frac{\sin(\theta - \psi) + R_1 \sin\theta}{R_2 \sin\psi - \sin(\theta - \psi)}$$

For the above, $\frac{d\psi}{d\theta} \left(\theta = 90, \psi = 90 \right) = 1.0 \quad \sqrt{\frac{d\psi}{d\theta}} \left(\theta = 90, \psi = -n \right) \approx -0.98$

Example (Shorter pushrod)

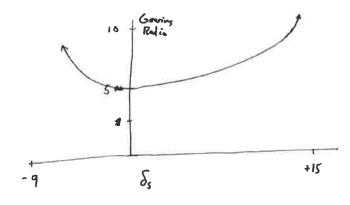


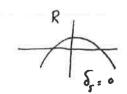
$$R_1 = 15$$
 $R_2 = 3$ $R_3 = 0.9974$

At
$$\delta_{s=0}$$
 We expect a georing ratio of 5, since $\frac{b}{d} = 5$

What are the limits of stick travel?

What is the georing retio at $S_s = 15^{\circ}$? $G \approx 216$ if $a + S_s = -9^{\circ}$ $G \approx 380$





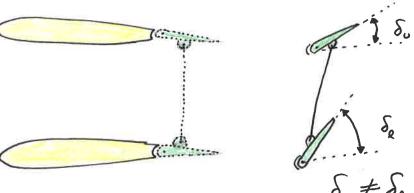


This indicates that

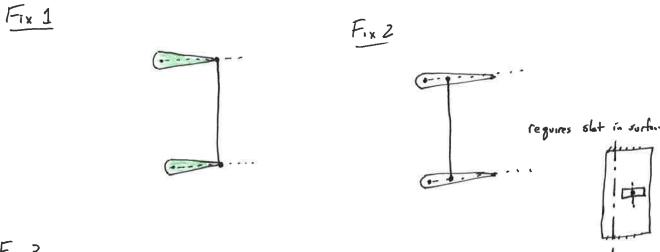
| 14f-ft at the surface
requires 200-300 ft-44

at the stick ... not happening ...

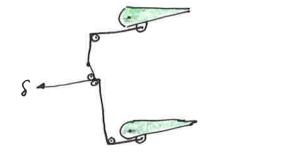
A common but flawed way to connect the ailerons on a biplene is:



The upper and lower surfaces don't have the same angle (other than $\delta u = \delta e = 0$).

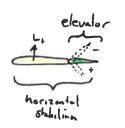


Fix 3



Elevator





previously, we trimmed our conceptual aircraft by adjusting it (the tail incidence agle)

Now, we add a hinged elevator to the horizontal Stab, which changes L and M.

$$\Delta C_L = C_L S_e S_e = \frac{dC_L}{dS_e} S_e$$

and
$$\Delta C_m = C_m S_e S_e = \frac{dC_L}{dS_e} S_e$$

elevator control power
$$\Delta C_m = C_m S_e S_e = \frac{dC_m}{dS_e} S_e$$

Sign convention

0 50

Applied to the aircraft pitching moment gives

Cm = Cmo + Cmo & + Cmse Se

Thus Case is usually a negative #.

Adjusting the clevator ellows for trumed flight

For the aircraft's total lift

$$\Delta C_{L} = \frac{dC_{L}}{d\delta_{e}} \delta_{e} = \frac{\eta}{\delta_{e}} \frac{\delta_{e}}{\delta_{e}} \delta_{e}$$

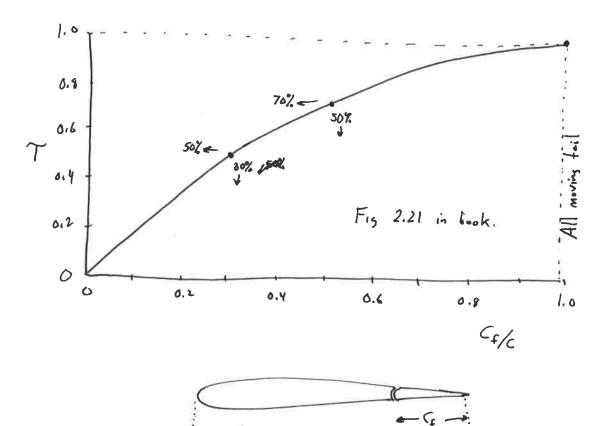
ref to Incremental wing 9 and lift caeff carea.

of total

Elevator Effectiveness

det = det dat de cont. de de constant = Cray T Angle of attack effections, Flop effectuences perameter For small angles, day a CLS How effective is a flop of Senerating lift compared to angle of attack

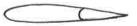
Flop Effectiveness Parameter



Notice that T is not a linear function of Copic.

Smeller chards (G/C) are compositively more effective

A 30% flop chord has 50% of the effectioners of a fully all movely to. 1



$$\Delta C_{m_0} \approx \frac{-l_+ \cdot L_+}{\frac{1}{2} \rho V^2 S_{\bar{c}_{\omega}}} = -V_H M \Delta C_{L_+}$$

combine with previewlt for Cus

The change in The change in the tou volume precious moment depends on dynamic pressure ratio wat flyp deflection

VH = 2+ 5+

" lift curve slope

+ fly effectumes

Q: How can you increase the emblack elevator control power?

Solve for Seaning

Flight Measurement of the neutral point

Find the slope of Strin wit Chin

$$\frac{d \, \delta_{hrin}}{d \, C_{uhrin}} = \frac{d}{d \, C_{hhin}} \left(\frac{C_{uhrin} \, C_{max} + C_{ubx} \, C_{mo}}{C_{ub} \, C_{ubx} \, C_{ubx} \, C_{ubx}} \right)$$

$$= \frac{C_{max}}{C_{ubx}} - C_{ubx} \, C_{mox} = \frac{C_{max}}{C_{ubx}} - C_{ubx} \, C_{mox}$$

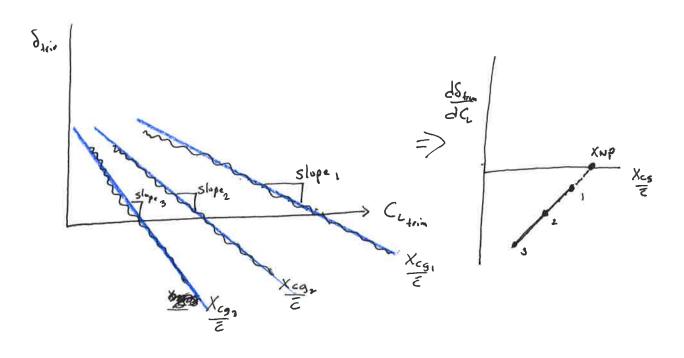
$$= \frac{C_{max}}{C_{ubx}} - C_{ubx} \, C_{mox} + C_{ubx} \, C_{mox}$$

$$= \frac{C_{max}}{C_{ubx}} - C_{ubx} \, C_{mox}$$

$$= \frac{C_{max}}{C_{ubx}} + C_{mox} \, \frac{S_{ubx}}{S_{ubx}} + C_{mox} \, \frac{V_{ubx}}{S_{ubx}} + C_{mox}$$

$$= \frac{C_{max}}{V_{ubx}} + C_{mox} \, \frac{S_{ubx}}{S_{ubx}}$$

$$= \frac{C_{max}}{V_{ubx}} + C_{ubx} + C_{mox} \, \frac{S_{ubx}}{S_{ubx}}$$

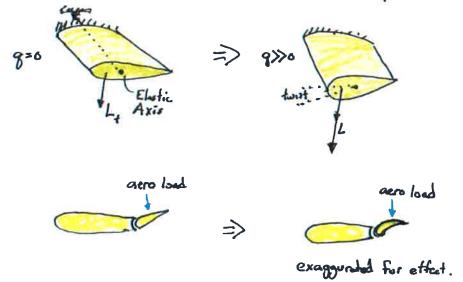


This can be done with multiple flights.

Other factors decreosing longitudinal stability

Aero elastics

The load on the stab varies with V^2 (since $g = \frac{1}{2}PV^2$). There will be deflections due to aero loads, these may increase or decrease stability depending on the structural response.



For light aircraft, the static margin even in an incompressible flow may strongly depend on the flight velocity

Read: tiny.cc /AEM 617 Tail Stability

Harry Clements designing the C-180

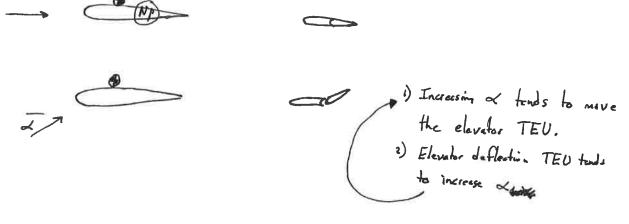
- · Suspected deflection in hors toil > reduced stab . I /near Vne
- · pencil lead to detect deflection
- · Not found!! Why? production changed design!

$$\left(\left|-\frac{C_{LSe}}{C_{Ld+}}\frac{C_{hot}}{C_{hSe}}\right|\right) = \left(\left|-\frac{(+)}{(+)}\frac{(-)}{(-)}\right|\right) = \left(\left|-\frac{(+)}{(+)}\frac{(-)}{(-)}\right|\right)$$

So the
$$\frac{X_{NP}}{\overline{c}} = \frac{X_{ac}}{\overline{c}} + \frac{C_{vol}}{C_{vol}} \left(\frac{1}{c} \right) - \frac{dc}{C_{vol}} + \frac{dc}{C_{vol}} \left(\frac{1}{c} \right) - \frac{dc}{C_{vol}} + \frac{dc}{C_{vol}$$

A floating clevator aircraft has an XNP nearer to Xee than the equivalent fixed stick aircraft.

Stick free is less stable



This is positive feedback.

Have you ever heard a pilot say
"The airplane flys well hands - aff."

They (polits) are saying the correct concept.

Lift tail a floatin, elevator

$$C_{L_{+}} = C_{L_{M_{+}}} \alpha_{+} + C_{L_{\delta_{e}}} \delta_{e}$$

$$= \left(C_{L_{M_{+}}} - C_{L_{\delta_{e}}} \frac{C_{L_{M_{+}}}}{C_{L_{\delta_{e}}}} \right) \alpha_{+} = C_{L_{M_{+}}} \left(1 - \frac{C_{L_{\delta_{e}}}}{C_{L_{M_{+}}}} \frac{C_{L_{M_{+}}}}{C_{L_{\delta_{e}}}} \right) \alpha_{+}$$

$$= \left(C_{L_{M_{+}}} - C_{L_{\delta_{e}}} \frac{C_{L_{M_{+}}}}{C_{L_{\delta_{e}}}} \right) \alpha_{+}$$

$$= \left(C_{L_{M_{+}}} + C_{L_{\delta_{e}}} \frac{C_{L_{M_{+}}}}{C_{L_{\delta_{e}}}} \right) \alpha_{+}$$

$$= \left(C_{L_{M_{+}}} + C_{L_{\delta_{e}}} \frac{C_{L_{M_{+}}}}{C_{L_{\delta_{e}}}} \right) \alpha_{+}$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{L_{\delta_{e}}} \frac{C_{L_{M_{+}}}}{M V_{H}} \left(C_{e} + i_{M_{+}} - i_{B} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{M_{+}}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(1 - \frac{1}{d_{M_{+}}} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{M_{+}}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(1 - \frac{1}{d_{M_{+}}} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(1 - \frac{1}{d_{M_{+}}} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(1 - \frac{1}{d_{M_{+}}} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(1 - \frac{1}{d_{M_{+}}} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(1 - \frac{1}{d_{M_{+}}} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(1 - \frac{1}{d_{M_{+}}} \right) \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{L_{\delta_{e}}} \frac{M V_{H}}{M V_{H}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) \right)$$

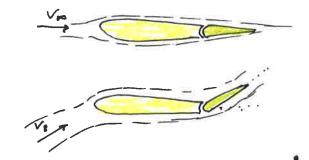
$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{M_{+}} \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{L_{M_{+}}} \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{1}}}{Z} \right) + C_{M_{+}} - C_{M_{+}} \right)$$

$$= \left(C_{L_{M_{+}}} \left(\frac{X_{e_{1}}}{Z} - \frac{X_{e_{$$

" Floating Elevator"



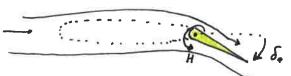
· Che is the hinge manent due to &



H is negative, the surface wonts to move TEU with "t" a

Chx LO

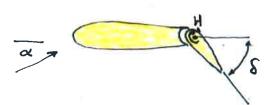
· Che is the hings moment due to deflection be



positive deflection tends to move surface back to zero deflection

Chse < 0

This effects stability!



A moment is necessary to maintain the control surface at S.

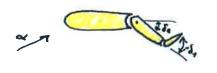
The pilot is connected to the surface in some way



$$S = f(stick onle)$$
 S_s
 $FQ_sS_e = HS_e \Rightarrow F = (\frac{S_e}{e_sS_s})H_e$

How much force can a pilot exert? How long? Hox V2; pilot is limited human! Constraints? Shuk position, structural stresses, ...

Trin Tab

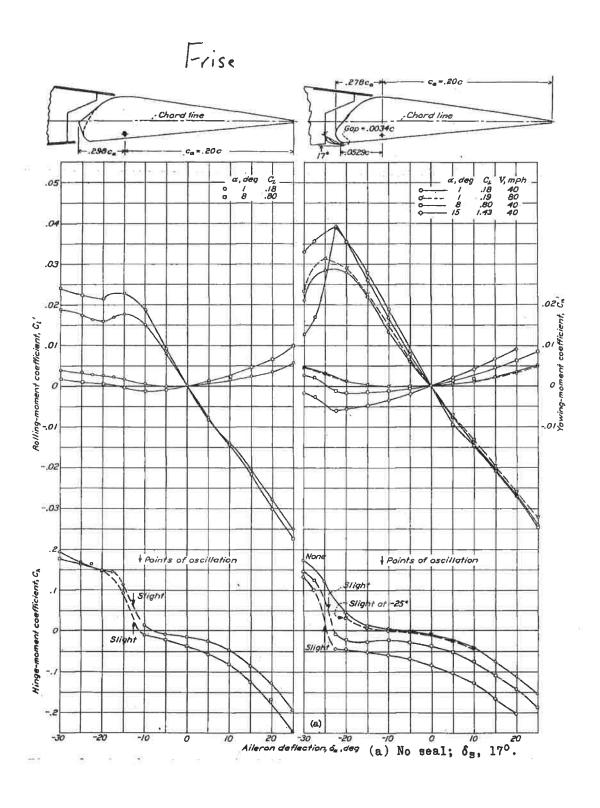


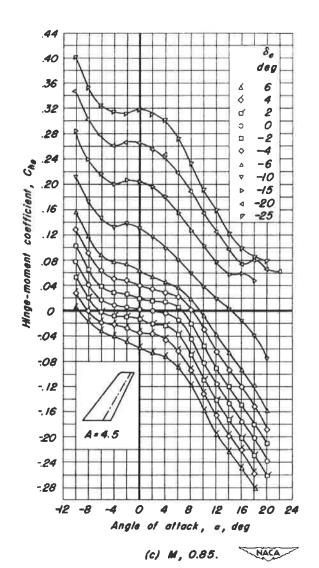
For the pilot to have zero stick force, Ch = 0

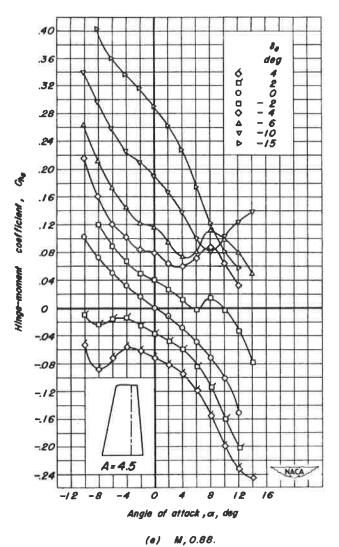
We (as public) can adjust of to ensure Cn = 0 for a porticular de required et a portueilor u.

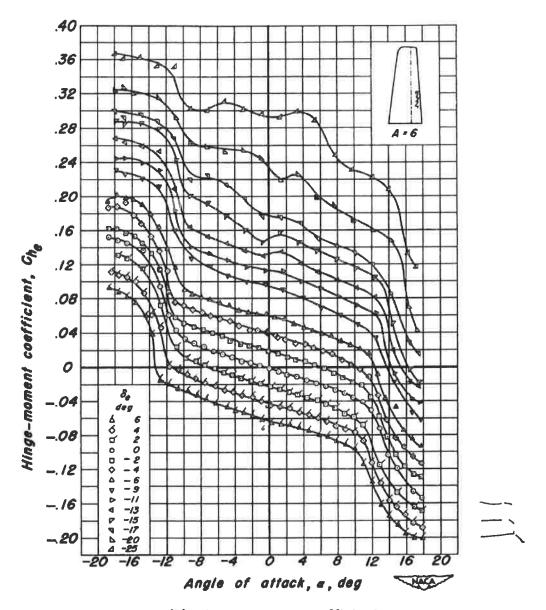
Stick free:

$$C_h = 0 = (C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0)$$
 $C_h = 0 = (C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0)$
 $C_h = 0 = (C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0)$
 $C_{h_0} = C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0$
 $C_{h_0} = C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0$
 $C_{h_0} = C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0$
 $C_{h_0} = C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0$
 $C_{h_0} = C_{h_0} + C_{h_0} + C_{h_0} + C_{h_0} = 0$
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 $C_{h_$





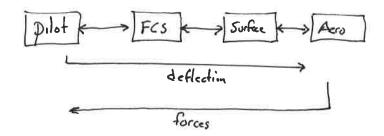




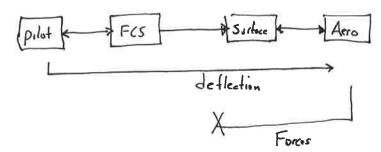
(b) Hinge-moment coefficient.

Reversible vs Irreversible Flight Control System.

Reversible



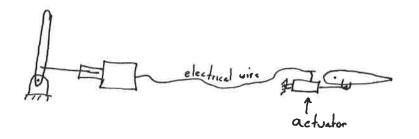
Irroversible



The pilot does not feel the aerodynamic forces!

Ex:





Fly by wire

Aerospatiale's SN-600 Corvette prototype has determined that over trimming of the aircraft's variable incidence tailplane probably is what caused the twin turbofan business jet to pitch over into an uncontrollable dive.

Aerospatiale officials are convinced the final accident report will clear the basic Corvette design and are accelerating development of two production aircraft and two test specimens. Flight tests with the new models - embodying configuration changes resulting from early prototype flight tests—are scheduled to begin late next year.

The aircraft should be certified by the end of 1973, in time to guarantee production delivery in early 1974. Three crewmen from the French civilian test center (CEV) were killed in the crash of the prototype, which occurred as they were doing high-altitude stalls (AW&ST Apr. 12, p. 53). The aircraft pitched over about 20 kts above normal stalling speed and entered a steep dive.

The only transmission from the pilots was a terse report from one of them that together they were unable to pull the aircraft out of the dive.

After long study of data from flight test recorder tapes, the investigators have determined that the pilot, who was flying the Corvette for the first time, apparently trimmed the tailplane to an excessive negative incidence, nose-up attitude during preparations for the stall tests. No stops had been installed to limit tailplane travel, because that portion of the flight envelope had not been fully explored.

All aircraft with variable-incidence tailplanes could encounter the same problem which caused the Corvette crash, according to several officials. When setting up the aircraft for the stall series, the pilot apparently put it in a configuration which ultimately reversed the action of the tailplane and elevator controls, they said.

The large-span flaps were deployed, creating a relative downward (or nose up) airflow over the tailplane. While trimming the tailplane, the pilot apparently released back pressure on the control yoke – as is general practice – and the elevator control surfaces moved to a nose-down position opposite that of the tailplane as they streamlined in the relative airflow, they said.

The resultant control surface configuration created a nose-down pitching moment before stall speed was reached, they said, and the deflected airflow generated by the flaps created aerodynamic pressures on the elevator controls which the pilots could not overcome. The Corvette has straight mechanical linkages without servo-controls in its flight control system.

To recover from the dive, the pilots would have had to move against their automatic reactions and trim the tailplane for nose-down, according to one official. This probably would have re-established the aerodynamic balance of the tailplane, they said. Raising the flaps also might have helped correct the control imbalance, they added.

Aerospatiale test pilots were aware that without stops the tailplane could be over-trimmed, they operated within certain limits while exploring the aircraft's envelope. How the CEV test pilot managed to trim the aircraft past these limits probably will not be determined.

Program officials said production aircraft will be equipped with stops which will make it impossible to establish an imbalanced configuration.

The French accident Investigating board has completed a study of the accident and has submitted its report to Aerospatiale and the French flight test center (CEV).

The official report said the cause of the accident was an "aerodynamic anomaly in the horizontal tail" and that the problem has been corrected on the new production design. The problem encountered basically was tailplane stall, according to one source, which was aggravated by a 45-deg. flap setting and high negative incidence setting of the horizontal tailplane. The aircraft pitched down about 20 kt, above normal stall speed.

The problem has been eliminated on production versions through a combination of previously planned lengthening of the fuselage – aimed primarily at improving aerodynamic drag – and smaller limits on movement of the three control surfaces involved.

Travel of the variable incidence tailplane has been reduced from +2 deg and -10 deg to +2 deg and -8 deg.

Elevator travel has been reduced from +25 deg and -15 deg to +20 deg and -10 deg. Flap deflection angle has been reduced from 45 deg. to 40 deg.

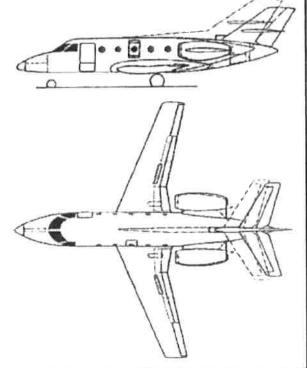
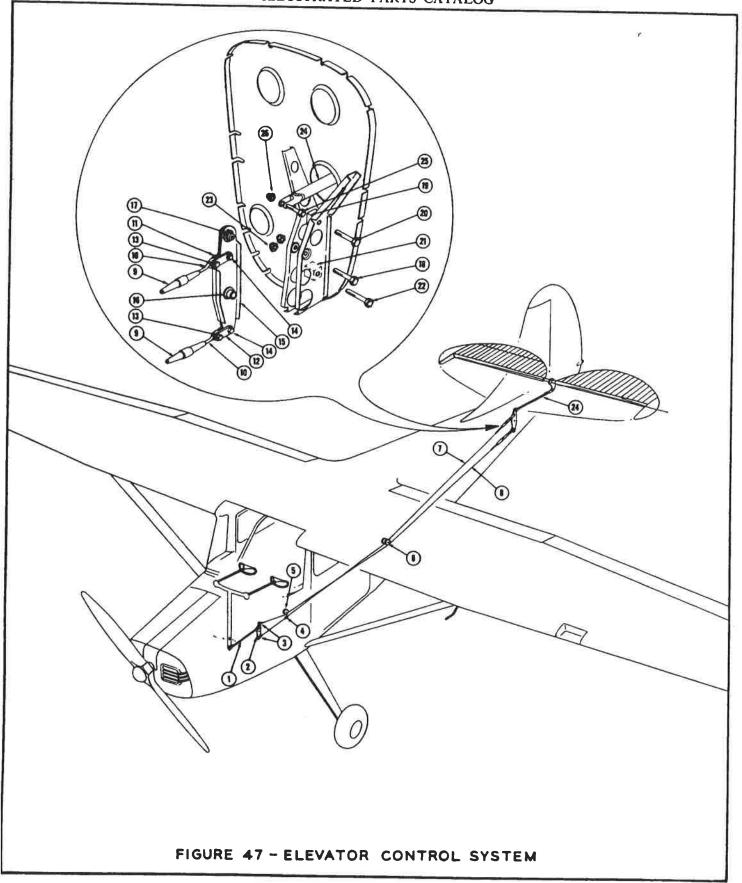
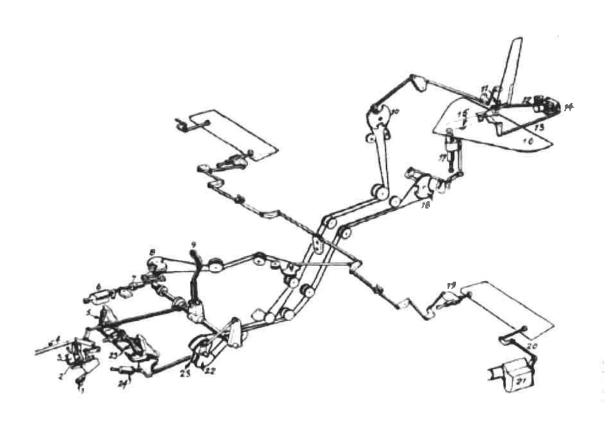


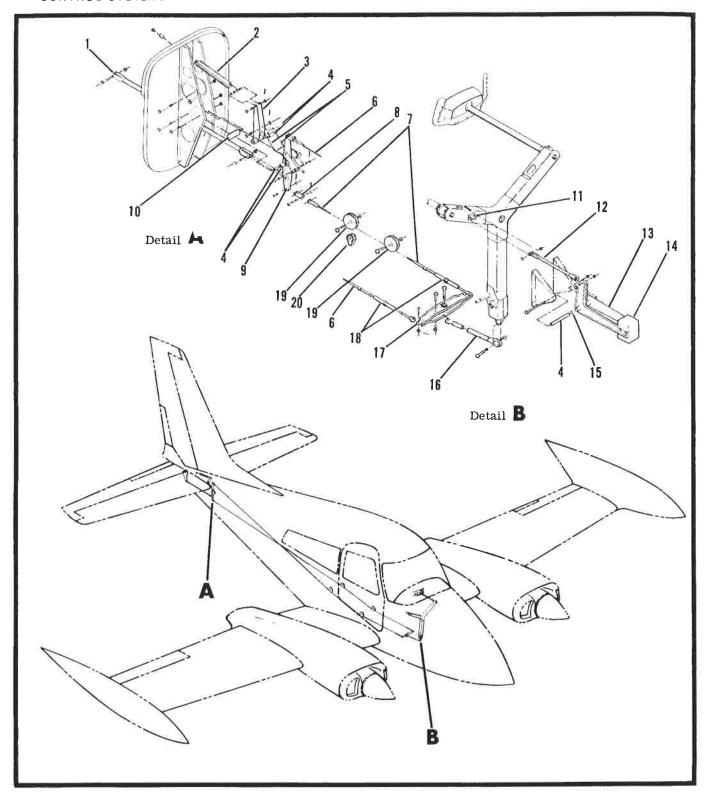
Figure 31.26 - Over-trimming cited in Corvette crash.

Source: Aviation Week and Space Technology, May 31 and October 18, 1971





AV-8 Harrier Flight Control System. Source: [MWF67]



- Elevator Push-pull Tube (Aft)
- Elevator Down Spring
 Down Spring Channel Assembly
- 4. Spacer
- 5. Down Spring Cable
- 6. Right Elevator Control Cable
- 7. Left Elevator Control Cable
- 8. Link
- 9. Elevator Bellcrank (Aft)
- 10. Bellcrank Stop
- 11. Bob-Weight Bracket
- 12. Push-pull tube
- 13. Bob-Weight Bellcrank
- 14. Bob-Weight
- 15. Bearing
- 16. Elevator Push-pull Tube (Forward)
- 17. Elevator Bellcrank (Forward)
- 18. Turnbuckle
- 19. Pulley
- 20. Cable Guard

Figure 6-2. Elevator Control System